

JAN 15/08

LET  $f(x) = \frac{p(x)}{q(x)}$  WHERE  $p(x)$  AND

$q(x)$  ARE POLYNOMIALS WITH NO  
COMMON FACTORS

1. FIND AND PLOT THE Y-INTERCEPT (IF ANY) BY EVALUATING  $f(0)$
2. FIND THE ZEROS OF THE NUMERATOR (IF ANY) BY SOLVING THE EQUATION  $p(x) = 0$ . PLOT THE X-INTERCEPTS
3. SKETCH THE ASYMPTOTES BY SOLVING THE EQUATION  $q(x) = 0$   
VERTICAL ASYMPTOTES
4. FIND AND SKETCH THE HORIZONTAL ASYMPTOTE BY USING THE RULE FROM BEFORE.
5. USE THE SIGN ANALYSIS
6. USE SMOOTH CURVES TO COMPLETE THE GRAPH

EG SKETCH  $f(x) = \frac{3}{x-2}$

FIND y-INT SET  $f(0)$

$$f(0) = \frac{3}{0-2} = -\frac{3}{2} \quad (0, -\frac{3}{2})$$

x-INT - NONE

VERTICAL ASYMPTOTE

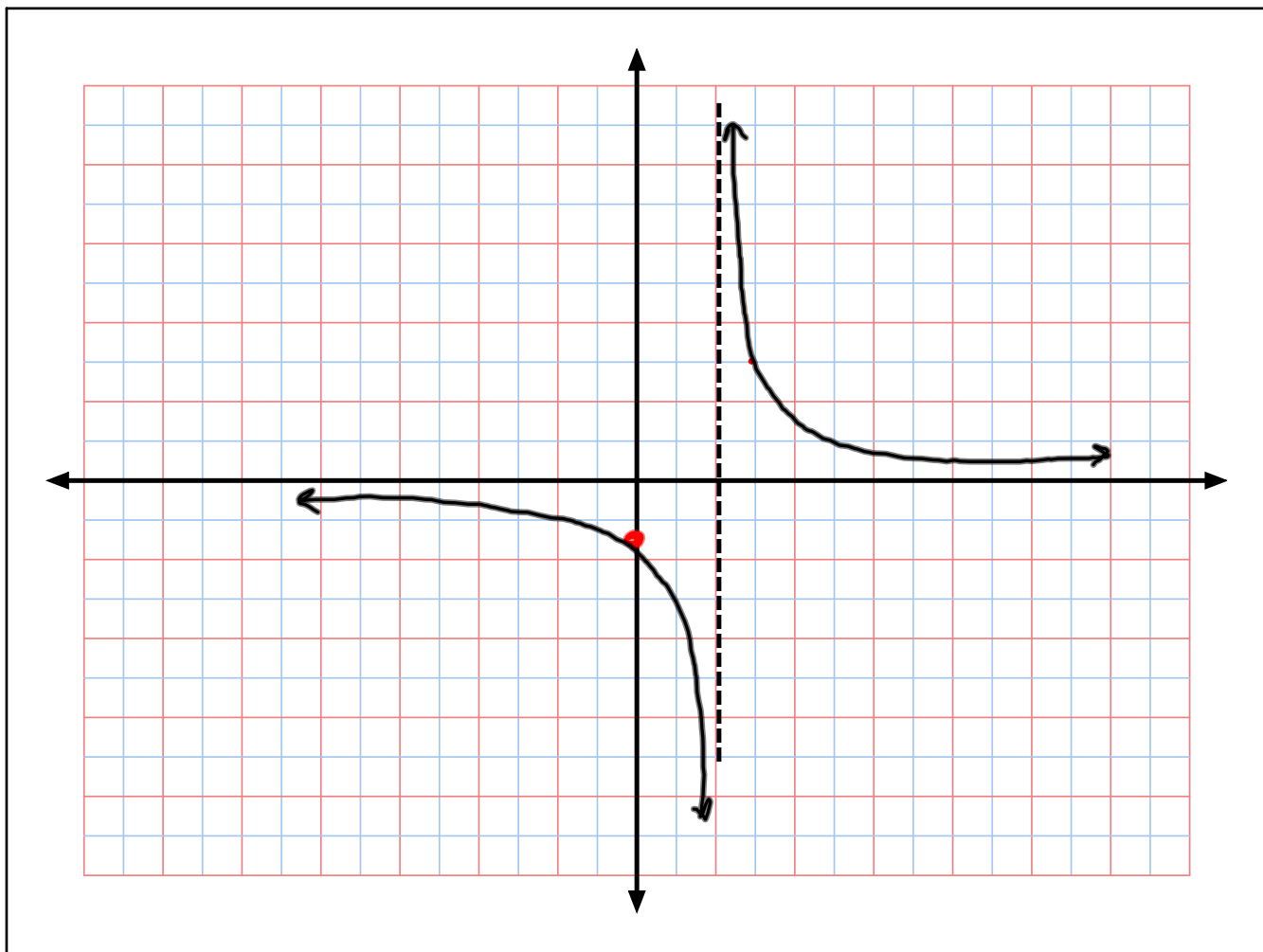
$$0 = x-2 \quad x=2$$

HORIZONTAL ASYMPTOTE

$$y=0$$

SIGN ANALYSIS

$x > 2$      $x = 3$     POSITIVE



EG. SKETCH  $f(x) = \frac{2x^2}{x^2 - 4}$

Y-INT  $f(0) = \frac{2(0)^2}{0 - 4} = 0$

X-INT  $2x^2 = 0 \quad x = 0$

VERT ASYMPTOTES  $x^2 - 4 = 0$   
 $(x-2)(x+2) = 0$   
 $2 \text{ and } -2$

HORI ASYMPTOTES

$$y = \frac{a}{b} = \frac{2}{1} = 2$$

CHECKING SIGNS

$x > 2 \quad x = 3 \quad \text{POSITIVE}$

